



INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(51) International Patent Classification⁴ :

H01Q 21/22, 21/00

A1

(11) International Publication Number:

WO 88/01106

(43) International Publication Date: 11 February 1988 (11.02.88)

(21) International Application Number: PCT/US87/01755

(22) International Filing Date: 21 July 1987 (21.07.87)

(31) Priority Application Number: 891,456

(32) Priority Date: 29 July 1986 (29.07.86)

(33) Priority Country: US

(71) Applicant: HUGHES AIRCRAFT COMPANY [US/US]; 7200 Hughes Terrace, Los Angeles, CA 90045-0066 (US).

(72) Inventors: LEE, Jar, Jueh ; 24 East Christamon, Irvine, CA 92720 (US). TANG, Raymond ; 567 Elinor Drive, Fullerton, CA 92635 (US).

(74) Agents: RUNK, Thomas, A. et al.; Hughes Aircraft Company, Post Office Box 45066, Bldg. C1, M/S A-126, Los Angeles, CA 90045-0066 (US).

(81) Designated States: DE (European patent), FR (European patent), GB (European patent), IT (European patent), JP.

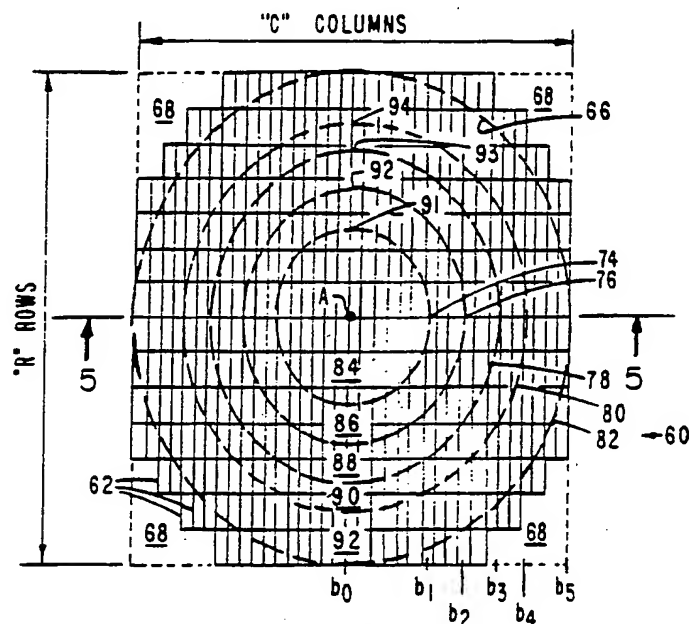
Published

*With international search report.**Before the expiration of the time limit for amending the claims and to be republished in the event of the receipt of amendments.*

(54) Title: LOW SIDELobe SOLID STATE ARRAY ANTENNA APPARATUS AND PROCESS FOR CONFIGURING AN ARRAY ANTENNA APERTURE

(57) Abstract

A low sidelobe, solid state array antenna apparatus comprises a large radiating aperture divided into a large number, N , of small, closely spaced radiating apertures, each small radiating aperture having associated therewith a radiating element and a linearly polarized solid state power module. The large radiating aperture is divided into M , preferably between (3) and about (10), differently sized, elliptically shaped, concentric radiating zones superimposed, for analysis purposes, upon another. Each such zone has an output voltage amplitude, E_i , and semi-major and semi-minor axes of respective lengths, a_i and b_i , each zone being considered separately in the far field equation: $G(\theta, \Phi) = [f(\theta, \Phi) (\hat{a}_\theta \cos \Phi - \hat{a}_\Phi \sin \Phi \cos \theta)]^2$, wherein $f(\theta, \Phi) = (I)$, $u_i = (II)$, $J_1(u_i)$ is the first order Bessel function, \hat{a}_θ and \hat{a}_Φ are unit vectors in the spherical coordinates and K_0 is the wave number associated with the radiated field. Using the far field equation, values of E_i , a_i and b_i for each zone are computed which result in the far field sidelobe peak gain being a minimum or being a specified number of dB, for example, at least about 30 dB, below the far field mainlobe gain. The values of E_i in overlapping zones are summed to establish the required voltage amplitudes of the underlying power modules associated with the N radiation apertures.



FOR THE PURPOSES OF INFORMATION ONLY

Codes used to identify States party to the PCT on the front pages of pamphlets publishing international applications under the PCT.

AT	Austria	FR	France	ML	Mali
AU	Australia	GA	Gabon	MR	Mauritania
BB	Barbados	GB	United Kingdom	MW	Malawi
BE	Belgium	HU	Hungary	NL	Netherlands
BG	Bulgaria	IT	Italy	NO	Norway
BJ	Benin	JP	Japan	RO	Romania
BR	Brazil	KP	Democratic People's Republic of Korea	SD	Sudan
CF	Central African Republic	KR	Republic of Korea	SE	Sweden
CG	Congo	LI	Liechtenstein	SN	Senegal
CH	Switzerland	LK	Sri Lanka	SU	Soviet Union
CM	Cameroon	LU	Luxembourg	TD	Chad
DE	Germany, Federal Republic of	MC	Monaco	TG	Togo
DK	Denmark	MG	Madagascar	US	United States of America
FI	Finland				

-1-

LOW SIDELOBE SOLID STATE ARRAY ANTENNA APPARATUS AND
PROCESS FOR CONFIGURING AN ARRAY ANTENNA APERTURE

1

BACKGROUND OF THE INVENTION

1. Field of the Invention

5 The present invention relates generally to the field of solid state, active aperture array antennas for radar, and more particularly to apparatus and methods for reducing sidelobe radiation by such antennas.

2. Discussion of the Background

10 Radar antennas are well known to radiate microwave radiation in an broad pattern which, for directed antenna, includes a narrow mainlobe and wide sidelobes of radiation. By common definition, the mainlobe is the central lobe of a directional antenna's radiation pattern, the sidelobes referring to the lesser lobes of progressively decreasing amplitude on both sides of the mainlobe and often extending rearwardly of the mainlobe.

15 Radar antenna aperture configuration generally determines the extent and relative magnitude of the associated sidelobes; however, the gain of the strongest one of the sidelobes is typically only about 1/64 that of the mainlobe. In terms of decibels, the strongest sidelobe gain is typically down about 18dB from the associated mainlobe gain. Gains of the other sidelobes

20

1 are usually considerably smaller than that of the
strongest sidelobe. Although sidelobe gain is typically
much smaller than mainlobe gain, because of the large
5 the small solid angle into which the mainlobe radiates,
typically about 25 percent of the total power radiated
by a uniformly illuminated radar antenna in the sidelobes.

Ordinarily, sidelobe radiation provides no useful
function and in addition to representing wasted radiating
10 power has other serious disadvantages. For example,
radar clutter from sidelobe returns increases the
difficulty of discriminating targets from background.
Another very significant disadvantage of sidelobe
radiation is that such radiation can, in a military
15 environment, be utilized by hostile forces for electroni-
cally jamming the radar and can also be used for positionally
locating and for guiding munitions to the radar. In this
regard, although mainlobe radiation is ordinarily much
greater than sidelobe radiation, its relatively small
20 solid angle of radiation and its directionality makes
mainlobe jamming, radar location and munitions direction
more difficult.

For these and other reasons, the reduction or
suppression of radar sidelobe radiation is, particularly
25 in military radar, important and military procurement
documents establishing rigid limits on sidelobe radiation
are not uncommon.

It is generally known that sidelobe radiation can
be suppressed in array-type radar antennas by "tapering"
30 the illumination over the aperture so that individual
radiation-emitting elements near the side edges of the
array radiate less energy do than other elements closer to
the center of the array. Power may, for example, be
individually applied to emitting elements of the array,
35 so that the radiation energy distribution across the
array, in at least one direction, is substantially Gaussian.

1 Radar arrays have, until quite recently, been
"passive" types in which each radiating element in the
array is provided power from a large, common power
source. For such passive arrays, tapering of the
5 radiation output, or, as it is sometimes termed, tapering
of array illumination, is comparatively easy to implement
by the use of restrictive branching from the power
source to the radiating elements, such that progressively
lower power is provided to elements further from the
10 array center.

More recently, however, there has been great
interest in developing active aperture arrays in which
each radiating element, or a subgroup of elements, in the
array is driven by a separate, small, solid state power
15 supply or module. Active arrays have numerous actual
and potential advantages over passive arrays. As an
example, the power modules of the active arrays, being
physically dispersed across the array, can be cooled
more efficiently and effectively than the single, high
20 power source of a corresponding passive array. Moreover,
within a large active array, a comparative large number
of power modules can fail or malfunction without
substantially impairing effectiveness of the antenna.
In contrast, failure or malfunction of the common power
25 source in a passive array incapacitates the entire
antenna.

According to theory, the providing of very smoothly
tapered illumination of passive array antennas should
be possible by the use of many (about 20 or more) different
30 groups of power modules, each group having a different
power output. In reality, however, the use of many
different power groups of modules is not practical
because such construction adds substantially to the cost
of producing the arrays and causes subsequent maintenance

1 and logistical support problems. As an illustration,
if twenty different power modules groups were to be
used in an array, supplies of all twenty different
type modules would have to be stocked wherever any
5 array maintenance and repair activities are expected to
be needed.

As a result of costs and problems involved with
using a large number of different power module groups in
active arrays, sidelobe reduction has generally been
10 attempted using only a relatively few different power
module groups which have heretofore provided only
coarsely tapered array illumination and relatively poor
side lobe reduction. The selection of power module
operating levels and arrangement has, so far as is
15 known to the present inventors, been previously made
merely by approximately fitting the resulting,
staircase-shaped distribution, having only a few steps,
to an optimal distribution which may, for example, be
in the bell-shape of a Gaussian distribution. Such
20 fitting of an actual, stepped distribution to an optimum
distribution curve has not heretofar, also so far as is
known to the present inventors, been based upon any
rigorous, systematic analysis and has not, therefore,
except possibly in isolated, accidental cases, resulted
25 in minimal sidelobes. Nor have such heretofore used
curve-fitting approaches enabled specific sidelobe
radiation levels to be predicted or designed to, as is
often required to meet procurement specifications.

30

35

1 As a result, to satisfy present and anticipated,
future low sidelobe requirements for solid state active
array antennas, improvements are required in the design
of such antennas, and specifically in processes for the
5 systematic selection of power module operating levels
and physical arrangements of power modules operating at
different power levels so as to provide low sidelobes.
It is to such a systematic approach for power
module operating levels and arrangements that the
10 present invention is directed.

SUMMARY OF THE INVENTION

 According to the present invention, a low sidelobe
solid state, phased array antenna apparatus, having a far
15 field mainlobe and sidelobe radiation pattern, comprises
an antenna aperture formed of a large number, N , of
small, closely spaced radiating apertures; N small,
linearly polarized radiating elements, each operatively
associated with a corresponding small radiating aperture
20 for radiating microwave energy therethrough; and a
number, preferably equal to the number, N , of solid
state power modules, each operatively associated with
at least one corresponding radiating element for providing
power thereto. The power modules are divided into a
25 number, M , of specifically arranged groups of modules,
the number M preferably being between 3 and about 10,
being more preferably between 3 and about 7 and being
most preferably equal to about 5. The output voltage
amplitude of each of the power modules is the same in
30 any group of modules, but is substantially different
in different groups of modules. The voltages amplitudes
of the power modules for the different module groups
and the boundaries of the M groups of modules are
selected so as to cause the far field sidelobe peak
35 gain to be down at least about 30dB from the associated
far field mainlobe gain of the array.

1 According to an embodiment, the M groups of power
modules are concentrically arranged around a central
point of the array so that the voltage amplitudes of
the power modules in the groups of modules decrease
5 with increasing distance from the array central point.
Also, according to an embodiment, the outer boundary of
each group of modules is elliptically shaped, having
respective semi-major and semi-minor axes a_i and b_i .
It should be pointed out that a circular boundary is
10 just a special case of this analysis wherein the aspect
ratio a_i/b_i is equal to one. Also, without loss of
generality, the shape of each elliptical boundary can be
chosen to have the same aspect ratio for convenience of
design. The output voltage amplitudes and the arrangement
15 of the groups of power modules are selected by treating
the module groups as being formed of, or comprising, a
superposition of M overlapping, elliptically-shaped
zones, each such zone having the same boundary as a
corresponding one of the module groups. Each of the M
20 zones has associated therewith a voltage amplitude, E_i .
The voltage amplitude of the power modules in each
group of modules is determined by treating the M module
voltage amplitudes as a superposition of the voltage
amplitudes, E_i , of the corresponding overlapped
25 zones. In conjunction therewith, the zone voltage
amplitudes, E_i , and the group boundary semi-major and
semi-minor axes, a_i and b_i , respectively, are selected
by application of the following expression for the far
field.

$$30 \quad G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_0 \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

$$\text{wherein } f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i,$$

$$35 \quad u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

1 $J_1(u_i)$ is the first order Bessel function,
 \hat{a}_0 and \hat{a}_ϕ are the unit vectors in the spherical
 coordinate system and k_0 is the wave number equal to
 $2\pi/\lambda$, with λ being the wavelength associated with
5 the radiated field.

 A corresponding process is provided for configuring
 low sidelobe array antennas, the process comprising
 forming an array antenna aperture from a large number, N ,
 of small radiating apertures, providing for each radiating
10 aperture a radiating element and a power module for
 supplying power to the radiating element, dividing the power
 modules into M different output voltage level groups
 and selecting the configuration of the groups of power
 modules and the output voltages amplitudes thereof so as
15 to cause the far field sidelobe gain to be down at least
 about 30dB from the corresponding far field mainlobe gain.

 The process includes treating the arrangement of the
 M groups of modules as a superposition of M overlapping,
 elliptical radiating zones having the same boundaries
20 as the power module groups, the output voltages amplitude
 for any group of modules being equal to the sum of the
 voltage amplitudes, E_i , of the superimposed radiating
 zones, the semi-major and semi-minor axes a_i and b_i
 of the zones and the voltage amplitude levels E_i
25 thereof being selected in accordance with the above
 equation to provide a far field sidelobe gain which is
 at least about 30dB down from the associated far field
 mainlobe gain.

30 BRIEF DESCRIPTION OF THE DRAWINGS

 A better understanding of the present invention
 may be had by considering the accompanying drawings
 in which:

 FIG. 1 is an exploded perspective of an exemplary
35 solid state, active array antenna with which the present
 invention may be used to advantage;

1 FIG. 2 is a pictorial drawing of the radiation pattern of a typical airborne radar, showing mainlobe and sidelobe portions of the radiation pattern;

5 FIG. 3 is a diagram depicting the coordinate system used to specify the coordinate of the far field relative to an radiating antenna;

10 FIG. 4 is a diagram depicting the manner in which a generally rectangular solid state active array antenna is divided into a series of M concentric, overlapping elliptical power module zones, each such zone having a different power level;

15 FIG. 5 is a diagram showing, relative to an array cross-section taken generally along line 5-5 of FIG. 4, how the aperture illumination taper is provided by superimposing different voltage levels of power modules in the different module zones of FIG. 4;

20 FIG. 6 is a diagram, similar to right hand portions of the diagram of FIG. 5, showing, for a particular array configuration and sidelobe radiation requirement, normalized power levels for five power module zones, the corresponding, normalized zone boundary dimensions being also indicated;

25 FIG. 7 is a graph plotting far field mainlobe and sidelobe gain vs angle from broadside axis for the conditions shown in FIG. 6; idealized, elliptical aperture zones being assumed; and

30 FIG. 8 is a graph plotting far field mainlobe and sidelobe gain vs angle from broadside axis for conditions in which stepped zone boundaries corresponding to actual module lattice configuration are assumed.

DESCRIPTION OF THE PREFERRED EMBODIMENT

There is shown in FIG. 1, in exploded form, an exemplary, solid state, active array antenna 10 of the general type with which the present invention may be used to advantage. Comprising antenna 10, which is shown as an aircraft-mounted type, are an aperture assembly 12, a cooling liquid plate assembly 14, a solid state power module assembly 16 and a stripline feed assembly 18. Included in aperture assembly 12 is a large number of small radiating elements 24, each of which has disposed therein a dielectric filler 26. Defined in a face 28 of aperture assembly 12 is a large number of openings 30, each of such openings being associated with one of radiating elements 24. Mounted on cooling plate assembly 14 are a number of loop assemblies 32, each of which is also associated with one of radiating elements 24. A large number of solid state power modules 34 comprise power module assembly 16, each such module preferably, but not necessarily, powering only a single associated radiating element 24.

The present invention is principally directed towards providing preselected voltage operating levels of power modules (corresponding to modules 34) and the physical arrangement of such modules in an assembly (corresponding to module assembly 16) so that the far field radiation from the antenna exhibits very low sidelobes. With respect to sidelobes, FIG. 2 illustrates a typical radiation pattern 38 associated with a radar carried by an aircraft 40. The airborne radar involved may, for example, comprise a solid state active array similar to array 10 depicted in FIG. 1. As shown in FIG. 2, radiation pattern 38 comprises a narrow, beam-shaped mainlobe 42 and smaller, fan-shaped sidelobes 44 on each side of the mainlobe. Sidelobes 44 comprise several different lobes 46 which fan out at different angles, α , relative to a main beam axis 48; typically

1 the sidelobes diminish in intensity as the angle, α
increases. It can further be seen from FIG. 2 that
some of lobes 46 extend rearwardly relative to mainlobe
42, the angles, α , associated therewith being greater
5 than 90°.

As more particularly described below, the present
invention relates to a process for configuring a solid
state, active array so that the far field sidelobe gain
is down a very substantial amount, preferably at least
10 about 30dB down, from the far field mainlobe gain. In
general, the reduced sidelobes provided by the present
invention is accomplished by tapering the radiating
illumination in a relatively few, precisely determined
steps.

15 For purposes of further describing the invention,
the more general case of a rectangular, solid state active
array 60, depicted in FIGS. 3-5; is considered. Array
60 corresponds generally to array 10 (FIG. 1), insofar
as general construction is concerned.

20 Also, for purposes of illustrating the invention, it
may be assumed that array 60 has rectangular dimensions
2a and 2b, and has R rows and C columns of linearly
polarized, rectangular radiating elements 62. Associated
with element 62 is a power module 64 (shown in phantom
25 lines).

It is, however, assumed, for purposes of simplifying
the following computations, that array 60 has an
elliptically (instead of a rectangular) radiating aperture
66, it having been determined by the present inventors
30 that array corner regions 68 contribute only negligibly
to sidelobes. For purposes of the following description,
the far field, G, associated with radiating aperture 66 is
considered, the far field at any point defined by
angles θ and ϕ being generally identified as $G(\theta, \phi)$
35 in FIG. 3.

1 A principal feature of the present invention is
the dividing, for analysis purposes, of radiating
aperture 66 into a relatively few, superimposed ellip-
tical zones around a central point "A", and the selection
5 of zone boundary axes a_i , b_i and the zone voltage
amplitudes, E_i , associated therewith in a manner
providing a tapered illumination of the aperture which
assures very low, far field sidelobes.

 Preferably the number of elliptical zones selected
10 varies between 3 and about 10 and more preferably
between 3 and only about 7. Insufficient illumination
tapering is considered to be provided using less than 3
zones and although smoother tapering can be provided by
use of more than about 7 zones, the cost of using more
15 than that number of different types of power modules is
costly and has moreover, been found by the present
inventors to be unnecessary for achieving very low
sidelobes. For specific purposes of illustrating the
invention, the number of zones shown and described is
20 5; however, any limitation to the use of about 5 zones
is neither intended nor implied.

 First through fifth concentric, progressively larger
elliptical zones 74, 76, 78, 80 and 82, respectively,
are thus selected, the zones having semi-major and
25 semi-minor axes equal, respectively, to a_1 , a_2 , a_3 ,
 a_4 , and a_5 and b_1 , b_2 , b_3 , b_4 , and b_5 (FIG. 4).
First zone 74 is the smallest zone and fifth zone 82 is
the largest zone and completely fills aperture 66,
dimensions a_5 and b_5 being, therefore, respectfully
30 equal to aperture dimensions a and b (FIG. 3).

 As can be seen from FIG. 5, which corresponds to
a transverse output voltage cross-section of array 60,
zones 74, 76, 78, 80 and 82 are, for analysis purposes,
considered as stacked (or superimposed) upon one another,
35 with the fifth, largest zone 82 at the bottom and the

1 first, smallest zone 74 at the top. Associated with
each zone 74, 76, 78 and 80 and 82 is a different
voltage amplitudes, E_i , amplitude E_1 being associated
5 with zone 74, E_2 with zone 76, E_3 with zone 78, E_4
with zone 80 and E_5 with zone 82. In regions where
two or more zones 74-82 overlap, the voltage amplitudes,
 E_i , are added to establish power module voltage. For
example, in a central, elliptical region 84, defined by
10 first zone 74, the combined voltage amplitude of the
stacked zones 74-82 required to be provided by underlying
power modules 60 is equal to $E_1 + E_2 + E_3 + E_4 + E_5$. In
an annular region 86 of second zone 76 outside of
first zone 74, the voltage amplitude required to be
provided by underlying power modules 60 is equal to
15 $E_2 + E_3 + E_4 + E_5$; in an annular region 88 of third
zone 78 outside of second zone 74, the voltage amplitude
required to be provided by the underlying power modules
is equal to $E_3 + E_4 + E_5$. In turn, in an annular
region 90 of fourth zone 80 outside of zone 78, the
20 voltage required to be provided by underlying power
modules 60 is $E_4 + E_5$; outside of zone 80, in an
annular region 92 of fifth zone 82, underlying power
modules 60 are required to provide a voltages amplitude
equal only to E_5 . However, by known principles of
25 superposition, each zone 74-82 can be treated separately
as providing only a single, corresponding voltage
amplitude E_1-E_5 .

30

35

The present process treats all zone axis dimensions, a_i , b_i , and zone voltage amplitudes, E_i , as independent variables. At least one set of values for these variables is computed which will provide, as may be required, either minimum sidelobes or a sidelobe gain which is a preselected number of dB less than the corresponding mainlobe gain. These independent variables a_i , b_i and E_i are computed, for numerous $G(\theta, \phi)$ points, by the equation:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \theta - \hat{a}_\phi \sin \theta \cos \phi)]^2, \quad (1)$$

$$\text{wherein } f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i, \quad (2)$$

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi}, \quad (3)$$

and further wherein $J_1(u_i)$ is the first order Bessel function, k_0 is the wave number associated with the radiation and \hat{a}_θ and \hat{a}_ϕ are the unit vectors in the spherical coordinate system.

To determine the optimum set of parameters (a_i , b_i , E_i) for low sidelobes, standard techniques of gradient search can be employed. In the optimization process an initial set of parameters is chosen as a starting point, and a present maximum sidelobe level (such as -30 dB) is selected as a performance criterion. Then the antenna far field pattern with the initial set of input parameters can be calculated by using Equation (1). Next the total power of all the sidelobes that exceed the present level, being defined as the error, is computed. After this a small variation of one of the parameters, either a positive or negative increment, is introduced and the error is recomputed. By examining the trend of the error, and hence the gradient (rate of change), one can decide

1 which way the following step of variation should be
implemented. The process is repeated for this parameter
until a local minimum in the error is obtained. By the
same procedure the iteration process is carried out for
5 all other parameters until the error is reduced to an
acceptable level. This optimization process can be
readily accomplished by using a computer. By way of
specific example, again with no limitations being
thereby intended or implied, the present inventors have
10 determined for M equal to 5 (that is, for five aperture
zones), the optimum zone boundaries, a_i , b_i , and
output voltage amplitudes, E_i . These values are shown
below in Table 1, wherein $a = a_5 = 1.3$ meters and
 $b = b_5 = .87$ meters, the sum of $E_1 + E_2 + E_3 + E_4 + E_5$
15 is normalized to 1.0 and the radiation frequency is
3.25 GHz. Furthermore, for simplicity of mathematical
derivation, the aspect ratio, b_i/a_i , for each zone is
identical to that of each other zone.

20

TABLE 1

	a_1	.44 m
	a_2	.68 m
	a_3	.88 m
25	a_4	1.01 m
	a_5	1.3 m
	b_1	.30 m
	b_2	.46 m
	b_3	.60 m
30	b_4	.68 m
	b_5	.87 m
	E_1	0.26
	E_2	0.22
	E_3	0.16
35	E_4	0.16
	E_5	0.20

1 FIG. 6, directly corresponds to the righthand
half of FIG. 5 and depicts, relatively to scale and for
the b_i dimensions normalized to $b = b_5 = 1$, the corres-
ponding, computed voltage amplitude, E_i , for each of
5 the five zones 74, 76, 78, 80 and 82. Also shown in
FIG. 6 is the dB value associated with the difference
in power level across each boundary: 2.62 dB with zone
74, 3.06 dB with zone 76, 3.1 dB with zone 78 and 5.11
dB with zone 80.

10 For the computed a_i , b_i , E_i values listed in
Table 1, there is plotted in FIG. 7 antenna pattern
gain (in dB) against elevation angle, θ as measured
from the broadside axis. From FIG 7 it can be seen
that the gains of all sidelobes 46 (shown shaded) are
15 down at least about 36dB from the peak (0°) gain of
mainlobe 42 over the entire visible radiation range.

In the foregoing, it has been assumed, for compu-
tations involving Equation 1, that the boundaries of
the five elliptical zones 74, 76, 78, 80 and 82 are
20 perfectly elliptical, as would be the case if there
were an infinite number of infinitely small power
modules 64 distributed over antenna elements 62. In
reality, however, each radiating zone intersects a
finite, though usually large, number of radiating
25 elements 62 so that the zone boundaries are more
accurately approximated by a discontinuous, stepped
shape, (FIG. 4). The question then arises as to which
of two adjacent zones the intersected radiating elements
62 (and corresponding power modules 64) should be
30 allocated and also whether allocation to one zone or
another makes any significant difference with respect
to sidelobe gain reduction.

1 To answer this question, a specific array pattern,
with actual element spacing and lattice structure taken
into account, was used by the present inventors to
compute aperture zone parameters a_i and b_i and voltage
5 amplitudes, E_i . For such purposes, the actual geometric
configuration of a proposed solid state radar array,
having an array size of 2.6 by 1.75 meters and having
1188 rectangular radiating elements, was assumed. It
was further assumed that the zone boundaries followed
10 actual boundaries of the radiating apertures. Values of
 a_i , b_i and E_i for minimum sidelobes were obtained for
such an array configuration by operation of Equation 1.
The computed gain VS elevation angle is plotted
in FIG. 8 which shows that the highest sidelobe gain is
15 down at least about 37 dB from the peak mainlobe gain.
A comparison of FIGS. 7 and 8 thus reveals that
although the sidelobe pattern is slightly different in
actual conditions (FIG. 8) as compared to that of the
idealized conditions (FIG. 7), the sidelobe gains are
20 nevertheless about the same in both cases.

Although there has been described above apparatus
and method for configuring a solid state, active array
antenna aperture so as to provide about a -30 to -35dB
peak sidelobe gain by using only a few different
25 power module groups, for purposes of illustrating the
manner in which the invention can be used to advantage,
it is to be understood that the invention is not limited
thereto. Accordingly, any and all variations and
modifications which may occur to those skilled in the
30 art are to be understood to be within the scope and
spirit of the invention as defined in the appended
claims.

CLAIMSWhat is claimed is:

- 1 1. A low sidelobe, solid state, phased array
antenna apparatus having a far field mainlobe and sidelobe
radiation pattern, the array antenna comprising:
- 5 a) an antenna aperture formed of a large
number, N, of small, closely spaced radiating apertures;
- b) a number, equal to the number N, of
linearly polarized radiating elements, each of which is
operatively associated with a corresponding one of the
small radiating apertures for radiating microwave energy
10 therethrough; and
- c) a number of solid state power modules,
each of which is operatively associated with at least
one of the radiating elements for providing power
thereto, the number of power modules being divided into
15 a number, M, of groups of power modules, the number M
being between 3 and about 10 and being much less than
the number N, the output voltage amplitudes of each of
the power modules being substantially the same for any
group of modules and being substantially different
20 for different groups of modules; the output voltage
amplitudes of the power modules for the M different
groups of modules and the boundaries of the M different
groups of modules being selected so as to cause the far
field sidelobe gain of the array to be down at least
25 about 30dB from the associated far field mainlobe gain
of the array.

1 2. The array antenna as claimed in Claim 1
wherein the number M is between 3 and about 7.

1 3. The array antenna as claimed in Claim 1 wherein
the number M is about 5.

1 4. The array antenna as claimed in Claim 1
wherein the M groups of power modules are concentrically
arranged around a central point of the array so that
the voltage voltage amplitudes of the power modules in
5 each of the M different groups of modules decrease with
increasing distance of the groups from said central
point.

1 5. The array antenna as claimed in Claim 4
wherein the outer boundary of each of the M groups of
power modules is elliptically shaped, each said boundary
having a semi-major axis of length a_i and a semi-minor
5 axis of length b_i , wherein the subscript "i" refers to
the ith boundary.

1 6. The array antenna as claimed in Claim 5 wherein
the output voltage amplitudes and the arrangement of said
M groups of power modules are selected by treating the
M module group arrangements as comprising a superposition
5 of M elliptically shaped, overlapping zones having the
same boundaries as corresponding ones of the M groups
of modules, each of said M zones having associated
therewith a different voltage amplitude E_i , the voltage
amplitude of the power modules in each of said M groups
10 being selected by adding the different voltage amplitudes,
 E_i , of the corresponding overlapping zones, wherein the
subscript "i" refers to the ith zone.

1 7. The array antenna as claimed in Claim 6
 wherein the voltage amplitudes, E_i , and semi-axis
 lengths, a_i and b_i , are selected by application of
 the following far field equation to cause the sidelobe
 5 gain to be down at least about 30dB from the mainlobe
 gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10 wherein $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$,

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15 $J_1(u_i)$ is the first order Bessel function,

\hat{a}_θ and \hat{a}_ϕ are unit vectors in the spherical coordinate
 system and k_0 is the wave number associated with the
 20 radiated field.

1 8. A low sidelobe, solid state phased array
 antenna apparatus having a far field mainlobe and sidelobe
 radiation pattern, the array antenna apparatus
 comprising:

5 a) an antenna aperture formed of a large number,
 N , of individual, closely spaced radiating apertures;

 b) a number, equal to the number N , of
 radiating elements, each of which is operatively associated
 with a corresponding one of the radiating apertures for
 10 radiating microwave energy therethrough; and

 c) a number of solid state power modules, each
 of which is operatively associated with at least one of
 the radiating elements for providing power thereto, the
 number of power modules being divided into a number, M ,

15 of groups of power modules, wherein the number M is
between 3 and about 7 and is much less than the number
 N , the M groups of power modules being arranged in a
concentric pattern around a central point of the array,
the output voltage amplitude of each of the power
20 modules being substantially the same in any one of the
 M groups of modules and being substantially different
in different groups of the modules, the M groups of
modules being arranged so that the voltage amplitudes
of the power modules in the groups of modules decreases
25 with increasing distance from the central point;

the output voltage amplitudes of the power
modules in the different groups of power modules
and the boundaries of the different groups of
power modules being selected, in combination, to
30 cause the far field peak sidelobe gain of the array
to be down at least about 30 dB from the corres-
ponding far field mainlobe gain of the array.

1 9. The array antenna as claimed in Claim 8
wherein the outer boundary of each of the M groups of
power modules is elliptical shaped, each said boundary
having a semi-major axis of length a_i and a semi-minor
5 axis of length b_i and wherein the M groups of modules
are treated as comprising a superposition of M ,
elliptically-shaped zones having the same boundaries as
corresponding ones of the groups of modules, each of
the M zones having associated therewith a different
10 voltage amplitude E_i , the voltages amplitude of the
power modules in each of said groups of modules being
a superposition of the different voltage amplitudes,
 E_i , of the overlapping zones associated with each of
the groups, wherein the subscript " i " refers to the i th
15 zone.

1 10. The array antenna as claimed in Claim 9
 wherein the amplitudes E_i and the semi-major and
 semi-minor axis lengths a_i and b_i , respectively,
 are selected by application of the following far field
 5 equation so as to cause the sidelobe gain to be down at
 least about 30dB from the mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10 wherein $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$,

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15 $J_1(u_i)$ is the first order Bessel function,

\hat{a}_θ and \hat{a}_ϕ are unit vectors in the spherical coordinate
 20 and k_0 is the wave number associated with the radiated field.

1 11. The array antenna as claimed in Claim 8 wherein
 the number M of groups of power modules is about 5.

1 12. A process for configuring a low sidelobe
 solid state, phased array antenna, the process comprising:

a) forming an array antenna aperture of
 a large number, N , of small, closely spaced radiating
 5 apertures;

b) providing for each of the small radiating
 apertures a radiating element, N radiating elements
 being thereby provided;

c) providing for each of the radiating elements
 10 a solid state power module;

d) dividing the power modules into M different power module groups, the number M being between 3 and about 10, and being much less than the number N;

15 e) selecting the configuration of the M groups of power modules and the output voltage amplitude of the power modules in each of the M groups of modules so as to cause the far field peak sidelobe gain to be down at least about 30dB from the corresponding far field mainlobe gain of the array.

1 13. The process as claimed in Claim 12 wherein the number M is between about 3 and about 7.

1 14. The process as claimed in Claim 12 wherein the number M is about 5.

1 15. The process as claimed in Claim 12 including
arranging the M groups of power modules concentrically
around a central point of the array and so that the voltage
amplitudes of the power modules in the M groups of modules
5 decreases with increasing distance from the central point.

1 16. The process as claimed in Claim 12 including
arranging the M groups of power modules so that the outer
boundaries thereof are substantially elliptically
shaped, each boundary having a semi-major axis
5 of length a_i and a semi-minor axis of length b_i , wherein
the subscript "i" refers to the ith boundary.

1 17. The process as claimed in Claim 16 including
 treating the M groups of power modules as comprising a
 superposition of M elliptically shaped, overlapping
 zones having the same boundaries as corresponding ones
 5 of the M groups of modules, each of the M zones having
 associated therewith a voltage amplitude, E_i , and
 including treating the voltage amplitude of the power
 modules in each of the M groups of power modules as an
 additive superposition of the voltages amplitudes, E_i ,
 10 of the corresponding overlapping zones, wherein the
 subscript "i" refers to the ith zone.

1 18. The process as claimed in Claim 17 including
 using the following far field equation to obtain values
 for the zone voltages amplitudes, E_i , and the zone semi-
 major and semi-minor axis lengths, a_i and b_i , which cause
 5 the far field sidelobe gain to be down at least about 30dB
 from the corresponding far field mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10 wherein $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$,

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15 $J_1(u_i)$ is the first order Bessel function,

\hat{a}_θ and \hat{a}_ϕ are unit vectors in the sperical coordinate
 20 and k_0 is the wave number associated with the radiated field.

1 19. A process for configurating a low sidelobe,
 solid state, phased array antenna, the process comprising:

- 5 a) providing, for an array antenna aperture, a large number, N, of small, closely spaced radiating apertures;
- b) providing for each of the small radiating apertures a radiating element, N radiating elements being thereby provided;
- 10 c) providing for each of the N radiating elements a solid state power module;
- d) dividing the power modules into M different power module groups, the number M being between 3 and about 7 and being much less than the number N, the output voltage amplitude of all the power modules in
15 any of the M groups of modules being substantially the same and the output voltage amplitudes of power modules in different groups of modules being different;
- e) arranging the M groups of power modules in a concentric pattern around a central point of the
20 array so that the output voltage amplitudes of the M groups of power modules decrease with increasing distance from said central point; and
- f) selecting the output voltage amplitudes of the power modules of the M groups of power modules and
25 the boundaries of the M groups of power modules so as to cause the far field sidelobe gain of the array to be down at least about 30dB from the corresponding far field mainlobe gain of the array.

- 1 20. The process claimed in Claim 19 including arranging the M groups of power modules so that the outer boundary of each said group is substantially elliptical in shape, each boundary having a semi-major axis of
5 length a_i and a semi-minor axis of length b_i and including treating each of the M groups of power modules as a superposition of M elliptically shaped, overlapping zones having the same boundaries as corresponding ones of the M groups of power modules, each of the M zones

10 having associated therewith a voltage amplitude, E_i , and including treating the voltage amplitude of each of the M groups of modules as an additive superposition of the voltage amplitudes, E_i , of the corresponding overlapping zones, wherein the subscript "i" refers to the i th zone.

1 21. The process as claimed in Claim 20 including using the following far field equation to obtain values of zone voltage amplitudes, E_i , and of the zone semi-major and semi-minor axis lengths, a_i and b_i , which cause
5 the sidelobe gain to be down at least about 30dB from the mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10 wherein $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$,

$$15 \quad u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

$J_1(u_i)$ is the first order Bessel function,

\hat{a}_θ and \hat{a}_ϕ are unit vectors in the spherical coordinate and k_0 is the wave number associated with the radiated field.

1 22. A process for configuring a low sidelobe, solid state phased array antenna, the process comprising:

a) providing, for an array antenna aperture, a large number, N , of small, closely spaced radiating
5 apertures;

b) providing for each of the N small radiating apertures a radiating element and a solid state power module, a number N of radiating elements and N power modules being thereby provided;

10 c) dividing the array antenna aperture into
a number, M, of differently sized, overlapping concentric
zones of elliptical shape, each of said zones having a semi-
major axis of length, a_i , and a semi-minor axis of length,
15 b_i ;

d) selecting, by use of the following far
field equation, values of E_i , a_i and b_i which cause the
far field sidelobe gain of the array to be down by at
least about 30dB from the corresponding far field
mainlobe gain;

20

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

25 wherein $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$,

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

30 $J_1(u_i)$ is the first order Bessel function,

\hat{a}_θ and \hat{a}_ϕ are unit vectors in the spherical coordinate,
 k_0 is the wave number associated with the radiated
field and the subscript "i" refers to the ith zone;

35 e) combining the E_i values for overlapping
areas of said zones and selecting the output voltages
amplitudes of power modules underlying the overlapped
zones to be equal to said combined E_i values.

1 23. The process as claimed in Claim 22 wherein
the number M is between 3 and about 10.

1 24. The process as claimed in Claim 22 wherein
the number M is about 5.

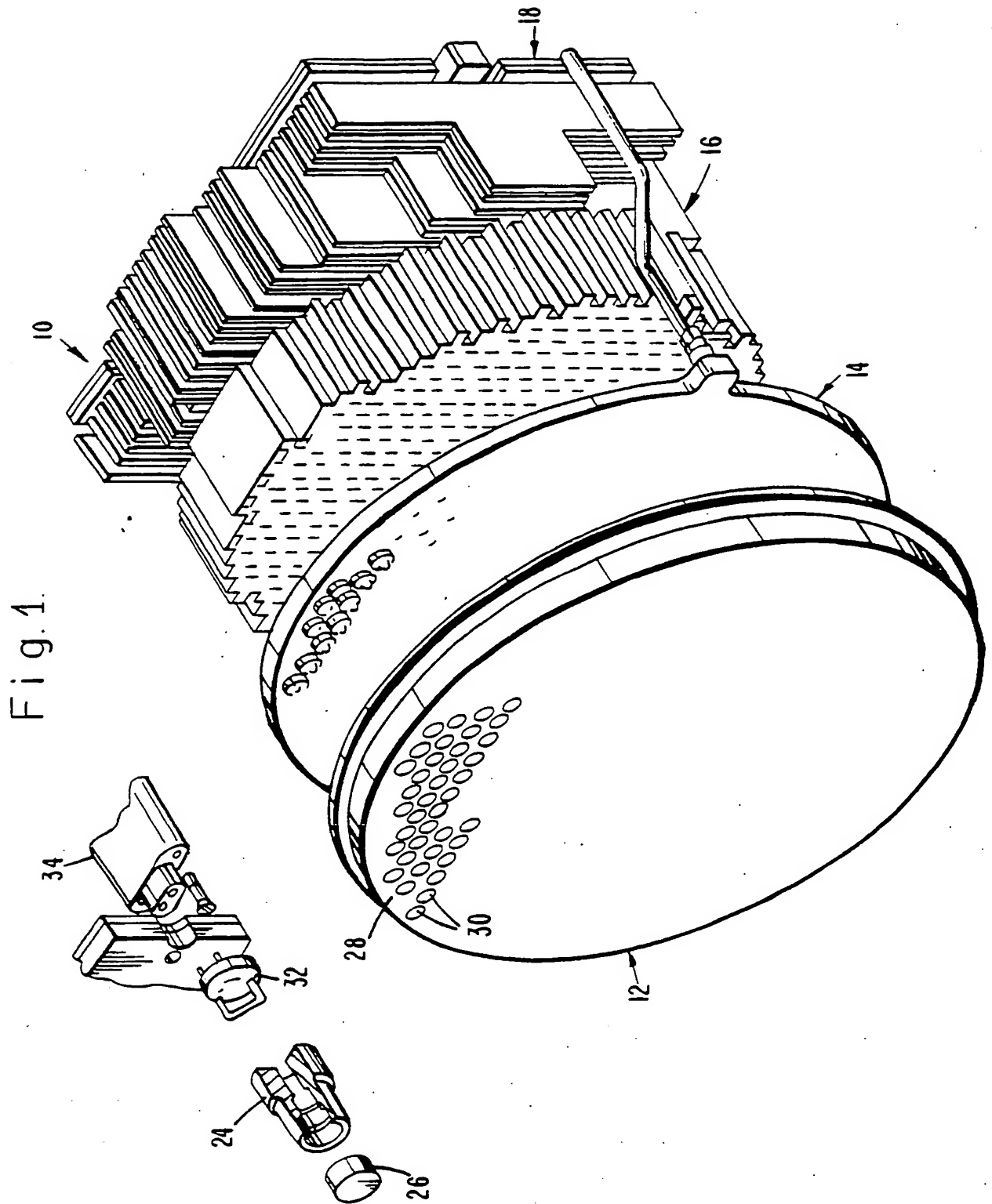


Fig. 2.

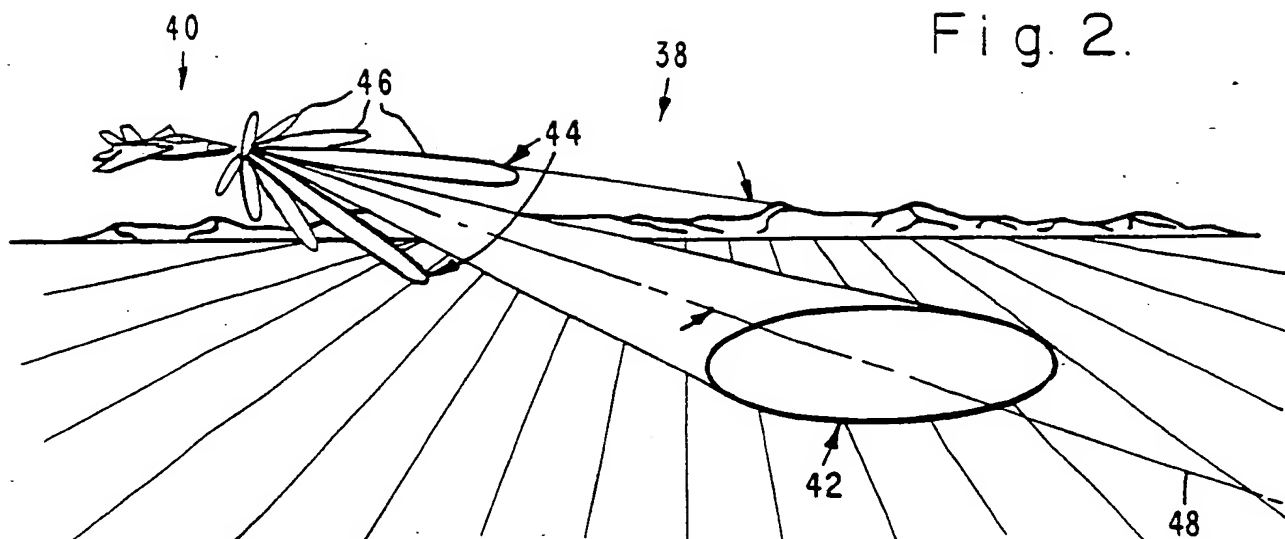
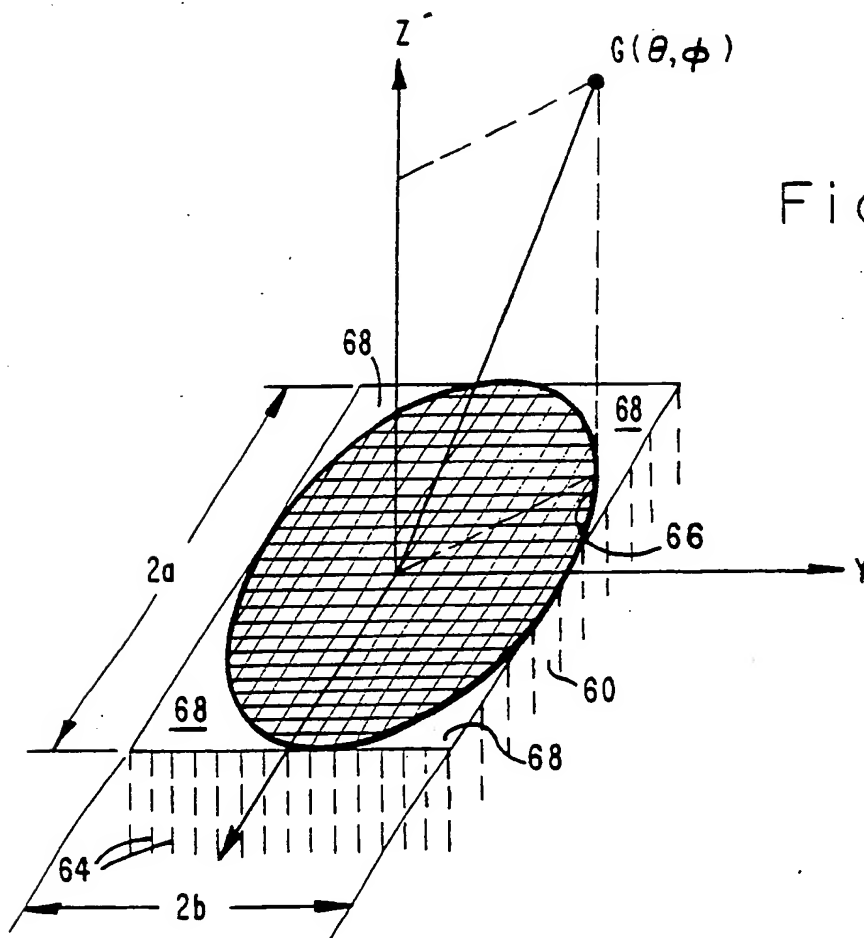


Fig. 3.



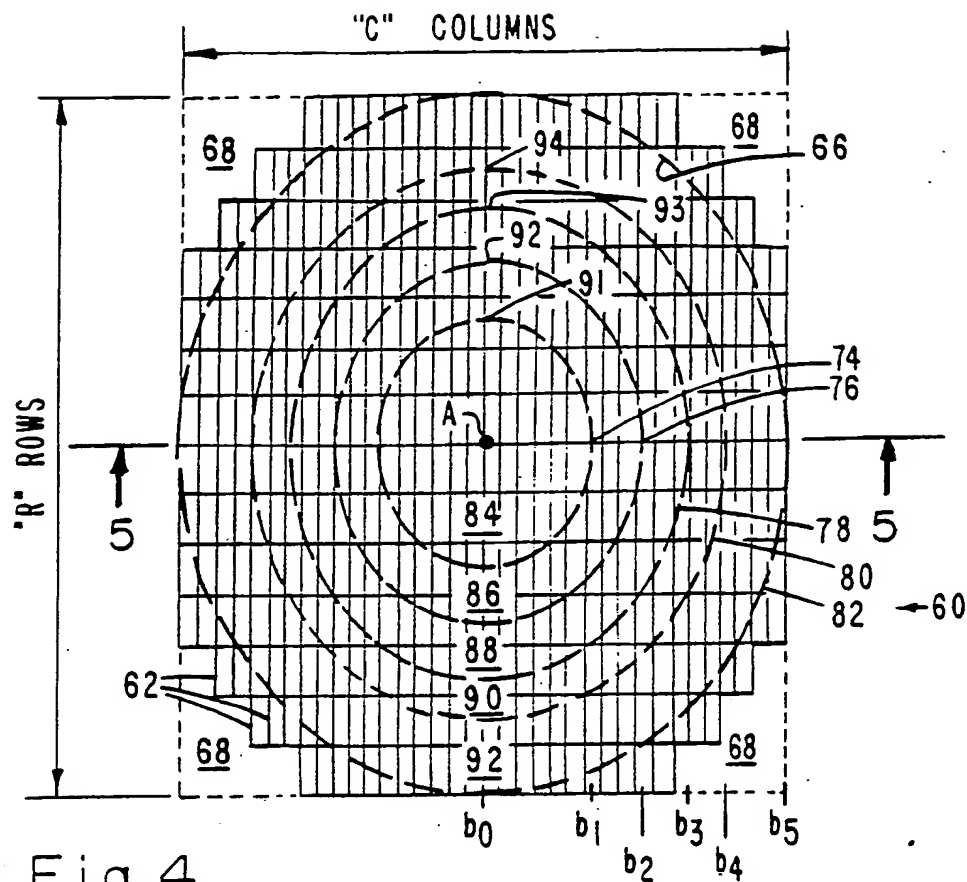
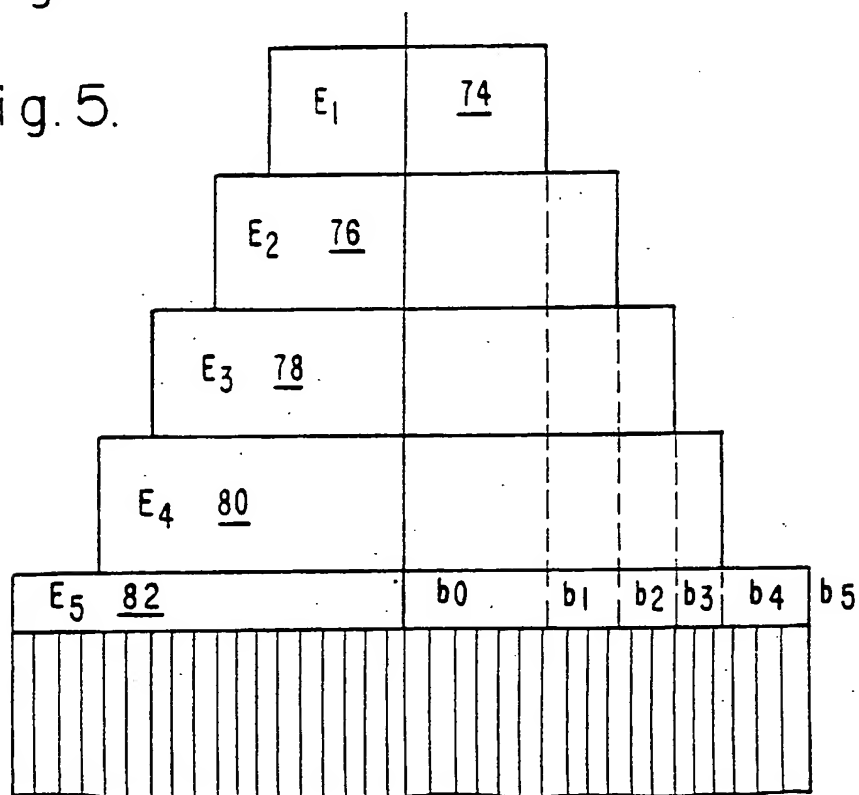


Fig. 4.

Fig. 5.



4/5

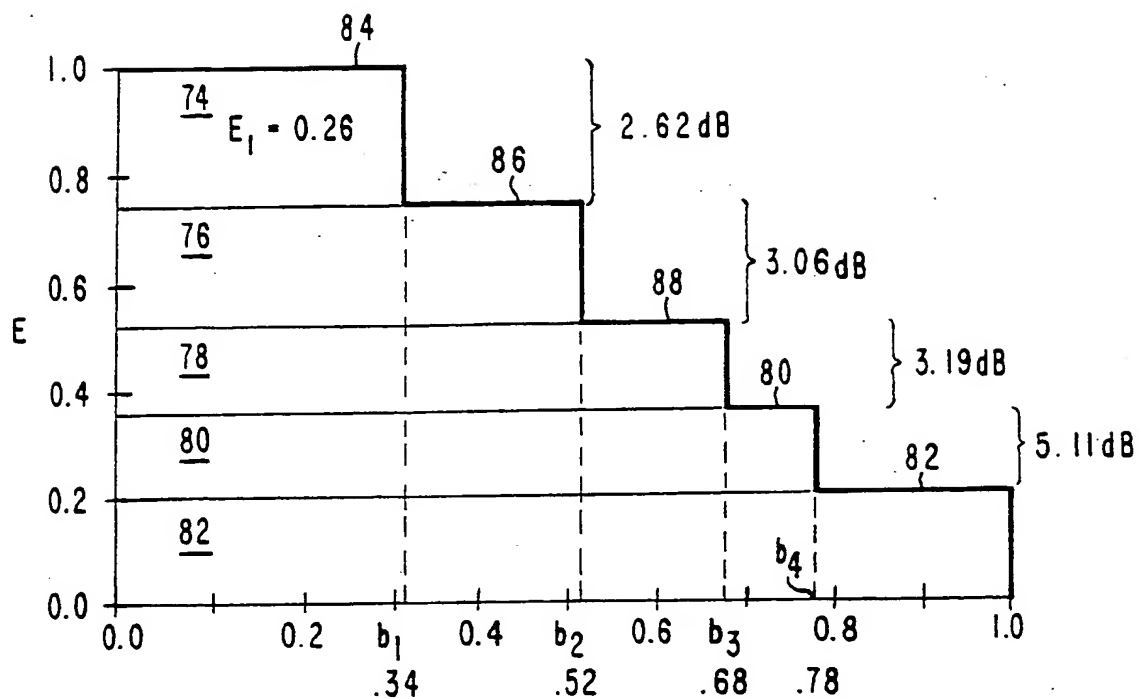
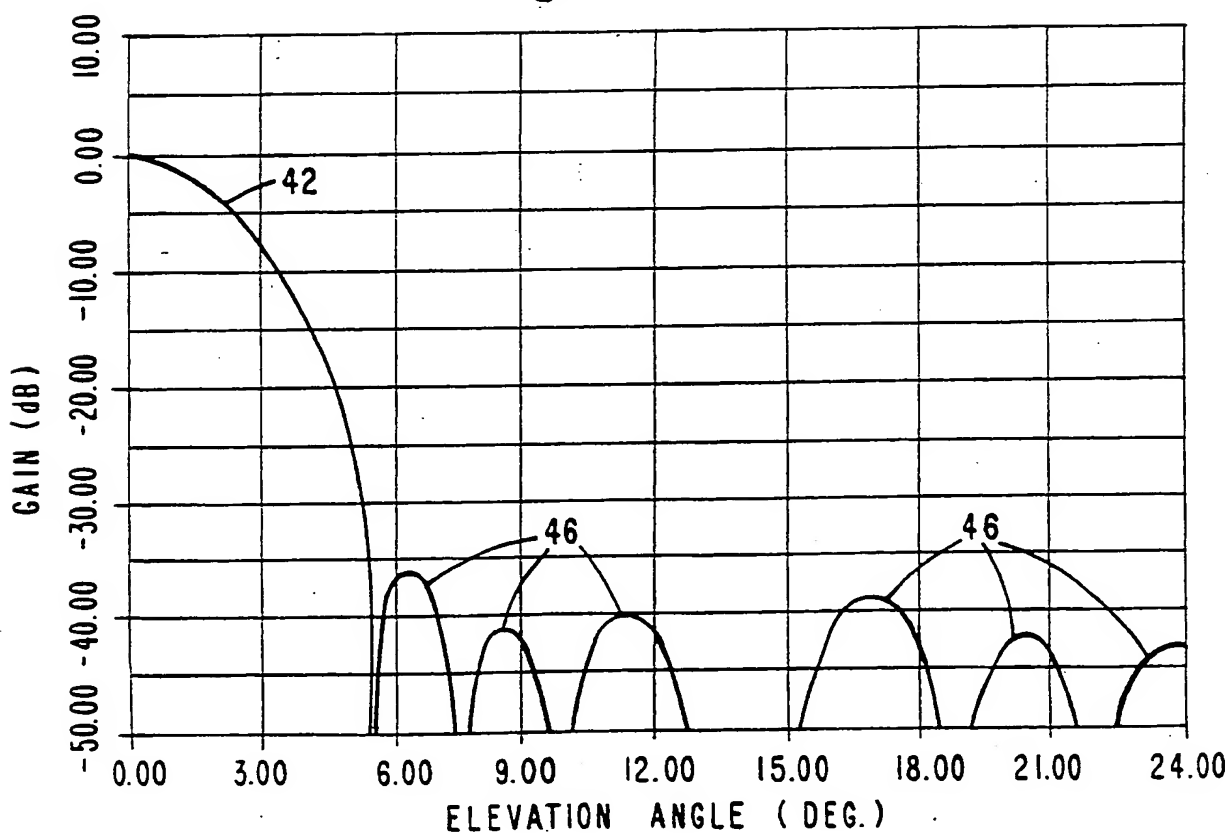


Fig. 6.

Fig. 7.



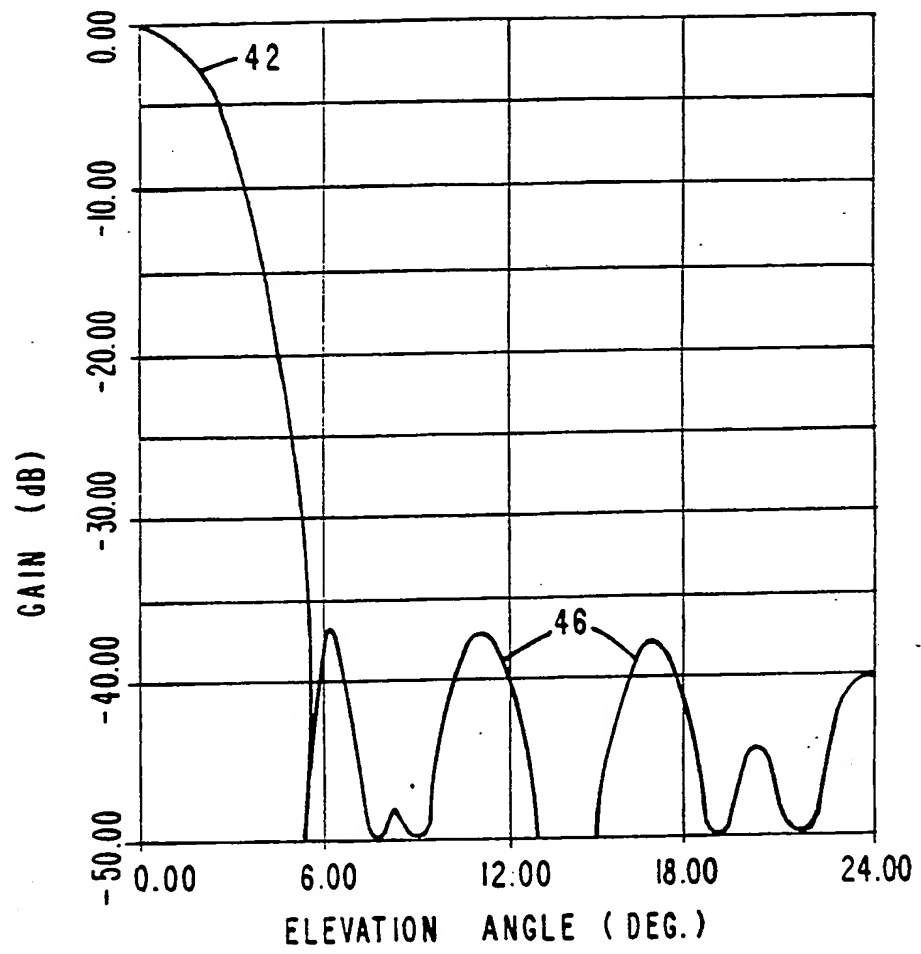


Fig. 8.

INTERNATIONAL SEARCH REPORT

International Application No PCT/US 87/01755

I. CLASSIFICATION OF SUBJECT MATTER (if several classification symbols apply, indicate all) ⁶ According to International Patent Classification (IPC) or to both National Classification and IPC IPC ⁴ : H 01 Q 21/22; H Q1 Q 21/00																	
II. FIELDS SEARCHED <div style="text-align: right; font-size: small;">Minimum Documentation Searched ⁷</div> <table style="width: 100%; border: none;"> <tr> <td style="width: 30%; border-bottom: 1px solid black; font-size: small;">Classification System</td> <td style="border-bottom: 1px solid black; font-size: small;">Classification Symbols</td> </tr> <tr> <td style="padding-top: 10px;">IPC⁴</td> <td style="padding-top: 10px;">H 01 Q</td> </tr> </table> <div style="text-align: center; font-size: x-small; margin-top: 10px;"> Documentation Searched other than Minimum Documentation to the extent that such Documents are included in the Fields Searched ⁸ </div>			Classification System	Classification Symbols	IPC ⁴	H 01 Q											
Classification System	Classification Symbols																
IPC ⁴	H 01 Q																
III. DOCUMENTS CONSIDERED TO BE RELEVANT ⁹ <table border="1" style="width: 100%; border-collapse: collapse; font-size: x-small;"> <thead> <tr> <th style="width: 10%;">Category ¹⁰</th> <th style="width: 70%;">Citation of Document, ¹¹ with indication, where appropriate, of the relevant passages ¹²</th> <th style="width: 20%;">Relevant to Claim No. ¹³</th> </tr> </thead> <tbody> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">Y</td> <td style="padding: 5px;"> 1982 IEEE MTT-S International Microwave Symposium Digest, 15-17 June 1982, Dallas, Texas, IEEE (New York, US), D.N. McQuiddy, Jr: "Solid state radar's path to GaAs", pages 176-178 see pages 176-177, left-hand column with figures 1-3 -- </td> <td style="text-align: center; vertical-align: top; padding: 5px;"> 1-4, 8, 12-15, 19 </td> </tr> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">Y</td> <td style="padding: 5px;"> US, A, 3760345 (HUGHES) 18-September 1973 see column 1, lines 35-54; column 2, line 30 - column 5, line 38 with figures 1-5 -- </td> <td style="text-align: center; vertical-align: top; padding: 5px;"> 1-4, 8, 12-15, 19 </td> </tr> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">A</td> <td style="padding: 5px;"> IEEE Transactions on Antennas and Propagation, volume AP-33, no. 8, August 1985, IEEE, (New York, US), R.L. Haupt: "Reducing grating lobes due to subarray amplitude tapering", pages 846-850 see pages 846, 849, sections I and II -- </td> <td style="text-align: center; vertical-align: top; padding: 5px;"> 1-4, 8, 12-15, 19 </td> </tr> <tr> <td colspan="2" style="text-align: right; padding: 5px;">./.</td> <td></td> </tr> </tbody> </table>			Category ¹⁰	Citation of Document, ¹¹ with indication, where appropriate, of the relevant passages ¹²	Relevant to Claim No. ¹³	Y	1982 IEEE MTT-S International Microwave Symposium Digest, 15-17 June 1982, Dallas, Texas, IEEE (New York, US), D.N. McQuiddy, Jr: "Solid state radar's path to GaAs", pages 176-178 see pages 176-177, left-hand column with figures 1-3 --	1-4, 8, 12-15, 19	Y	US, A, 3760345 (HUGHES) 18-September 1973 see column 1, lines 35-54; column 2, line 30 - column 5, line 38 with figures 1-5 --	1-4, 8, 12-15, 19	A	IEEE Transactions on Antennas and Propagation, volume AP-33, no. 8, August 1985, IEEE, (New York, US), R.L. Haupt: "Reducing grating lobes due to subarray amplitude tapering", pages 846-850 see pages 846, 849, sections I and II --	1-4, 8, 12-15, 19	./.		
Category ¹⁰	Citation of Document, ¹¹ with indication, where appropriate, of the relevant passages ¹²	Relevant to Claim No. ¹³															
Y	1982 IEEE MTT-S International Microwave Symposium Digest, 15-17 June 1982, Dallas, Texas, IEEE (New York, US), D.N. McQuiddy, Jr: "Solid state radar's path to GaAs", pages 176-178 see pages 176-177, left-hand column with figures 1-3 --	1-4, 8, 12-15, 19															
Y	US, A, 3760345 (HUGHES) 18-September 1973 see column 1, lines 35-54; column 2, line 30 - column 5, line 38 with figures 1-5 --	1-4, 8, 12-15, 19															
A	IEEE Transactions on Antennas and Propagation, volume AP-33, no. 8, August 1985, IEEE, (New York, US), R.L. Haupt: "Reducing grating lobes due to subarray amplitude tapering", pages 846-850 see pages 846, 849, sections I and II --	1-4, 8, 12-15, 19															
./.																	
<div style="display: flex; justify-content: space-between; font-size: x-small;"> <div style="width: 45%;"> <p>¹⁰ Special categories of cited documents:</p> <p>"A" document defining the general state of the art which is not considered to be of particular relevance</p> <p>"E" earlier document but published on or after the international filing date</p> <p>"L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)</p> <p>"O" document referring to an oral disclosure, use, exhibition or other means</p> <p>"P" document published prior to the international filing date but later than the priority date claimed</p> </div> <div style="width: 45%;"> <p>"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention</p> <p>"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step</p> <p>"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art</p> <p>"Z" document member of the same patent family</p> </div> </div>																	
IV. CERTIFICATION <table style="width: 100%; border: none;"> <tr> <td style="width: 50%; border-bottom: 1px solid black; font-size: small;">Date of the Actual Completion of the International Search</td> <td style="width: 50%; border-bottom: 1px solid black; font-size: small;">Date of Mailing of this International Search Report</td> </tr> <tr> <td style="text-align: center; padding-top: 10px;">3rd November 1987</td> <td style="text-align: center; padding-top: 10px;">- 1 DEC 1987</td> </tr> <tr> <td style="border-bottom: 1px solid black; font-size: small;">International Searching Authority</td> <td style="border-bottom: 1px solid black; font-size: small;">Signature of Authorized Officer</td> </tr> <tr> <td style="text-align: center; padding-top: 10px;">EUROPEAN PATENT OFFICE</td> <td style="text-align: center; padding-top: 10px;">M. VAN MOL </td> </tr> </table>			Date of the Actual Completion of the International Search	Date of Mailing of this International Search Report	3rd November 1987	- 1 DEC 1987	International Searching Authority	Signature of Authorized Officer	EUROPEAN PATENT OFFICE	M. VAN MOL							
Date of the Actual Completion of the International Search	Date of Mailing of this International Search Report																
3rd November 1987	- 1 DEC 1987																
International Searching Authority	Signature of Authorized Officer																
EUROPEAN PATENT OFFICE	M. VAN MOL																

III. DOCUMENTS CONSIDERED TO BE RELEVANT (CONTINUED FROM THE SECOND SHEET)		
Category *	Citation of Document, with indication, where appropriate, of the relevant passages	Relevant to Claim No
A	US, A, 3553706 (CHARLTON) 5 January 1971 see column 1, lines 11-23; figures 1a-c and 5	1,5-12, 16-19,22- 24
	--	
A	US, A, 3811129 (HOLST) 14 May 1974 see abstract; column 6, lines 10-36	1-4,8,12- 15,19,22
	--	
A	US, A, 4052723 (MILLER) 4 October 1977 see abstract and figures 2-5	1,8,12 19,22

ANNEX TO THE INTERNATIONAL SEARCH REPORT ON

INTERNATIONAL APPLICATION NO.PCT/US 87/01755 (SA 18210

This Annex lists the patent family members relating to the patent documents cited in the above-mentioned international search report. The members are as contained in the European Patent Office EDP file on 12/11/87

The European Patent Office is in no way liable for these particulars which are merely given for the purpose of information.

Patent document cited in search report	Publication date	Patent family member(s)	Publicat date
US-A- 3760345	18/09/73	None	
US-A- 3553706	05/01/71	None	
US-A- 3811129	14/05/74	None	
US-A- 4052723	04/10/77	None	

For more details about this annex :
see Official Journal of the European Patent Office, No. 12/82